

Grab a worksheet from the front table and Warm Up on A - F. Don't work past F.

## Classwork - Finding Missing Angle in Triangles

**Warm Up:** Determine whether (Yes or No) the side lengths and angle measures can be those of a triangle.

### SHOW WORK

#### Side Lengths

A) 8 in, 3 in, 10 in

$$\begin{aligned} 8 + 3 &> 10 \\ 11 &> 10 \end{aligned} \quad \text{Yes}$$

B) 7 cm, 12 cm, 5 cm

$$\begin{aligned} 7 + 5 &> 12 \\ 12 &\not> 12 \end{aligned} \quad \text{No}$$

C) 14 ft, 6 ft, 7 ft

$$\begin{aligned} 6 + 7 &> 14 \\ 13 &\not> 14 \end{aligned} \quad \text{No}$$

#### Angle Measures

D)  $144^\circ$ ,  $13^\circ$ ,  $23^\circ$

$$144 + 13 + 23 = 180^\circ$$

Yes

E)  $47^\circ$ ,  $29^\circ$ ,  $92^\circ$

$$47 + 29 + 92 = 168^\circ$$

No

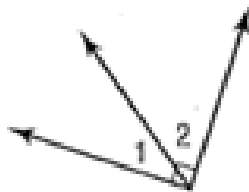
F)  $75^\circ$ ,  $22^\circ$ ,  $83^\circ$

$$75 + 22 + 83 = 180^\circ$$

Yes

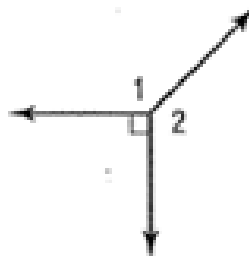
Classify each pair of angles as *complementary*, *supplementary*, or *neither*.

1.



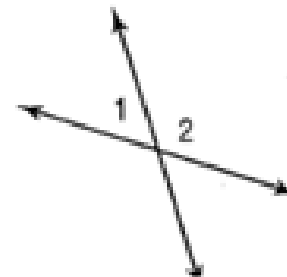
Complementary

2.



Neither

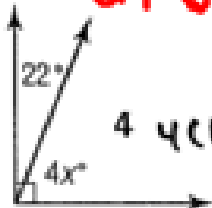
3.



Supplementary

ALGEBRA Write and solve an equation to find the value of  $x$  in each figure. Then find the measure of the missing angle. SHOW WORK AND LABEL

4.



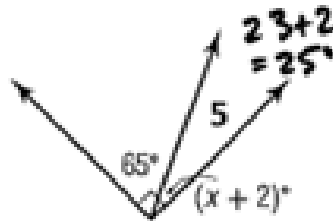
$$22 + 68 = 90$$

$$4 \cdot 4(17) =$$

$$\begin{array}{r} 4x + 22 = 90 \\ - 22 \quad -22 \\ \hline 4x = 68 \\ \frac{4}{4} \quad \frac{68}{4} \\ x = 17 \end{array}$$

$$x = \underline{17} \quad \angle 4 = \underline{68^\circ}$$

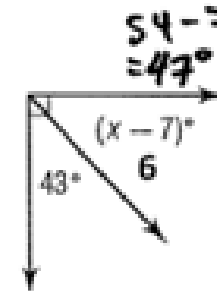
5.



$$\begin{array}{r} x + 2 + 65 = 90 \\ x + 67 = 90 \\ - 67 \quad -67 \\ \hline x = 23 \end{array}$$

$$x = \underline{23} \quad \angle 5 = \underline{25^\circ}$$

6.



$$\begin{array}{r} x - 7 + 43 = 90 \\ x + 36 = 90 \\ - 36 \quad -36 \\ \hline x = 54 \end{array}$$

$$x = \underline{54} \quad \angle 6 = \underline{47^\circ}$$

7.

$$\begin{aligned}
 &156-5 \\
 &7 = 151^\circ \\
 &(x-5)^\circ \\
 &29^\circ \\
 &x-5+29=180 \\
 &x+24=180 \\
 &\quad -24 \quad -24 \\
 \hline
 &x=156
 \end{aligned}$$

$x = \underline{156}$      $\angle 7 = \underline{151^\circ}$

8.

$$\begin{aligned}
 &7(10)=70 \\
 &110^\circ \quad 7x^\circ 8 \\
 &7x+110=180 \\
 &\quad -110 \quad -110 \\
 \hline
 &7x=70 \\
 &\quad \frac{7}{7} \quad \frac{70}{7} \\
 &x=10
 \end{aligned}$$

$x = \underline{10}$      $\angle 8 = \underline{70^\circ}$

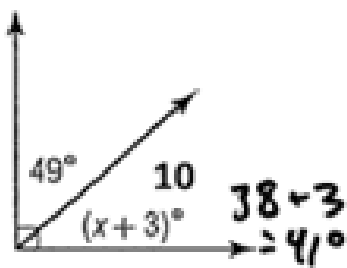
9.

$$\begin{aligned}
 &9 \quad 104+4=108^\circ \\
 &72^\circ \quad (x+4)^\circ \\
 &13 \\
 &x+4+72=180 \\
 &x+76=180 \\
 &\quad -76 \quad -76 \\
 \hline
 &x=104
 \end{aligned}$$

$x = \underline{104}$      $\angle 9 = \underline{108^\circ}$   
 $\angle 13 = \underline{72^\circ}$

$151^\circ + 29^\circ = 180^\circ$

10.



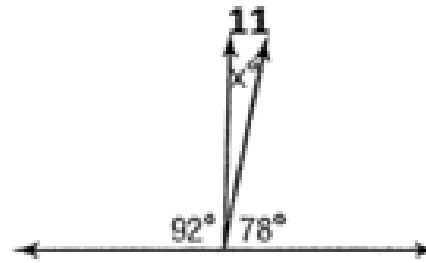
$$x + 3 + 49 = 90$$

$$x + 52 = 90$$

$$\begin{array}{r} -52 \\ -52 \end{array}$$

$$\hline x = 38$$

11.



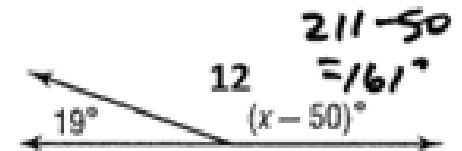
$$92 + x + 78 = 180$$

$$x + 170 = 180$$

$$\begin{array}{r} -170 \\ -170 \end{array}$$

$$\hline x = 10$$

12.



$$x - 50 + 19 = 180$$

$$x - 31 = 180$$

$$\begin{array}{r} +31 \\ +31 \end{array}$$

$$\hline x = 211$$

$$x = \underline{38} \quad \angle 10 = \underline{41^\circ}$$

$$x = \underline{10} \quad \angle 11 = \underline{10^\circ}$$

$$x = \underline{211} \quad \angle 12 = \underline{161^\circ}$$

13. ALGEBRA If  $\angle C$  and  $\angle D$  are supplementary, and the measure of  $\angle D$  is  $45^\circ$ , what is the measure of  $\angle C$ ?

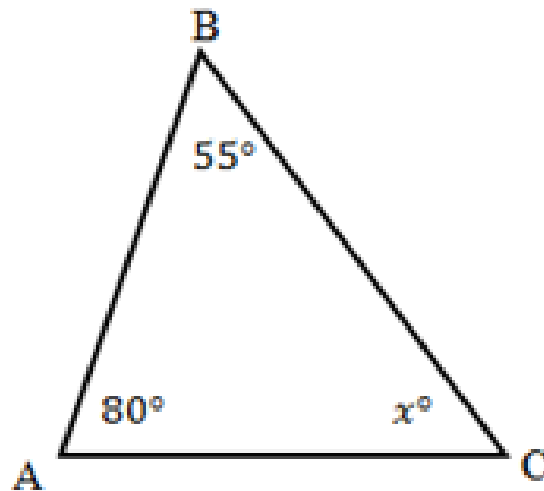
$$\angle C + 45^\circ = 180^\circ$$

$$\begin{array}{r} -45 \\ -45 \end{array}$$

$$\hline \angle C = 135^\circ$$

When finding the whether the angles above in problems D – F, we determined if the 3 angles would form a triangle by checking if the angles added up to 180 degrees. We can use this information to write equations that solve missing angles.

$$\text{Equation} \rightarrow \angle A + \angle B + \angle C = \underline{180^\circ}$$



Insert the degree values that you know and then solve for the missing angle.

SHOW WORK

$$80 + 55 + C = 180$$

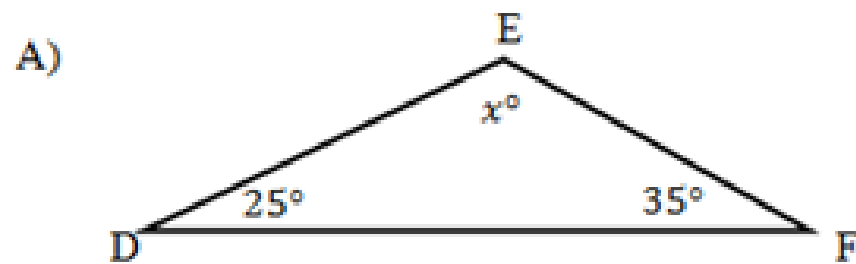
$$135 + C = 180$$

$$-135$$

$$-135$$

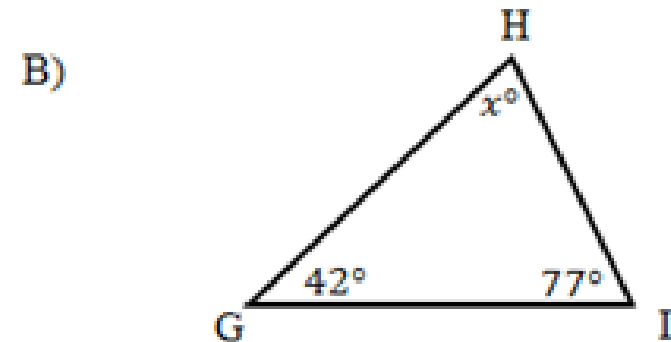
$$\underline{\underline{C = 45^\circ}}$$

Practice: Write and then solve an equation to find the missing angles of each of triangles below. LABEL



Equation  $\rightarrow 25 + x + 35 = 180$   
 $x + 60 = 180$

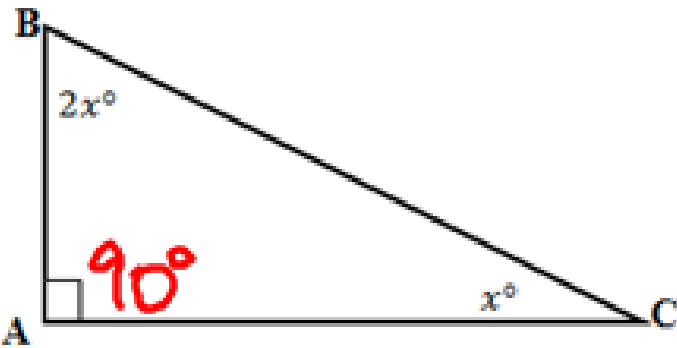
Missing Angle =  $\underline{120^\circ} - 60 - 60$   
 $x = 120^\circ$



Equation  $\rightarrow 42 + 77 + x = 180$   
 $119 + x = 180$

Missing Angle =  $\underline{61^\circ} - 119 - 119$   
 $x = 61^\circ$

### Writing and Solving Equations to Find the Value of $x$ .



Write an equation to find the value of  $x$ .

Equation  $\rightarrow 2x + x + 90 = 180$

Solve the equation you wrote above. Remember to solve, **the equation must be completely simplified.** SHOW WORK

Find the missing angles by inserting what you found  $x$  to be into the expressions.

$$m\angle B = \underline{60^\circ} \quad m\angle C = \underline{30^\circ}$$

$$x = \underline{30}$$

$$2(30) = 60^\circ$$

$$90 + 60 + 30 = 180 \checkmark$$

$$2x + x + 90 = 180$$

$$3x + 90 = 180$$

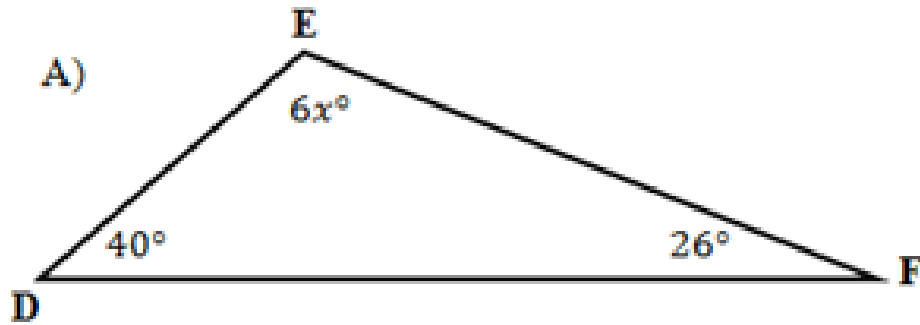
$$\begin{array}{r} 3x + 90 = 180 \\ -90 \quad -90 \\ \hline \end{array}$$

$$3x = 90$$

$$\begin{array}{r} 3x = 90 \\ \underline{3} \quad \underline{3} \end{array}$$

$$x = 30$$

Practice: Write and solve an equation to find the value of  $x$ . Then find the measurement of the missing angle(s).



Equation  $\rightarrow$

$$x = \underline{19} \quad m\angle E = \underline{114^\circ}$$

$$6x + 40 + 26 = 180$$

$$6x + 66 = 180$$

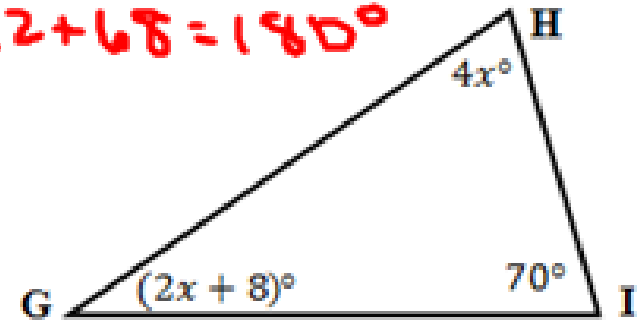
$$\begin{array}{r} -66 \\ -66 \end{array}$$

$$\frac{6x}{6} = \frac{114}{6}$$

$$x = 19$$

$$70 + 42 + 68 = 180^\circ$$

B)



Equation  $\rightarrow$

$$x = \underline{17} \quad m\angle G = \underline{42^\circ} \quad m\angle H = \underline{68^\circ}$$

$$2x + 8 + 4x + 70 = 180$$

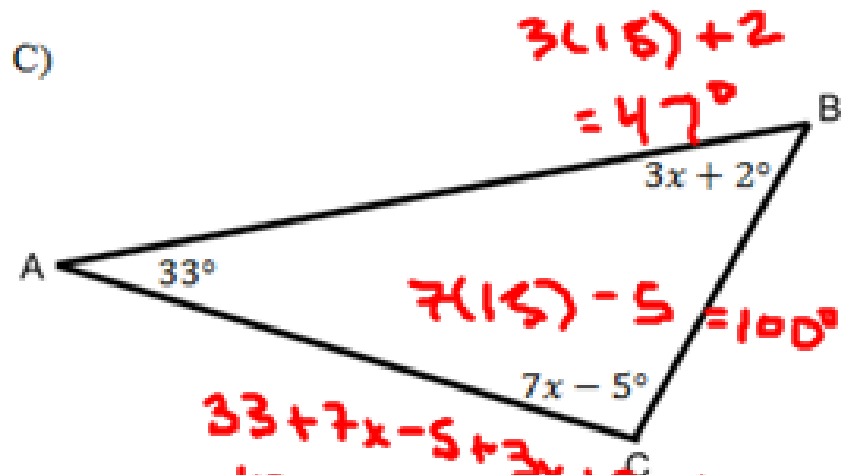
$$6x + 78 = 180$$

$$\begin{array}{r} -78 \\ -78 \end{array}$$

$$\frac{6x}{6} = \frac{102}{6}$$

$$x = 17$$





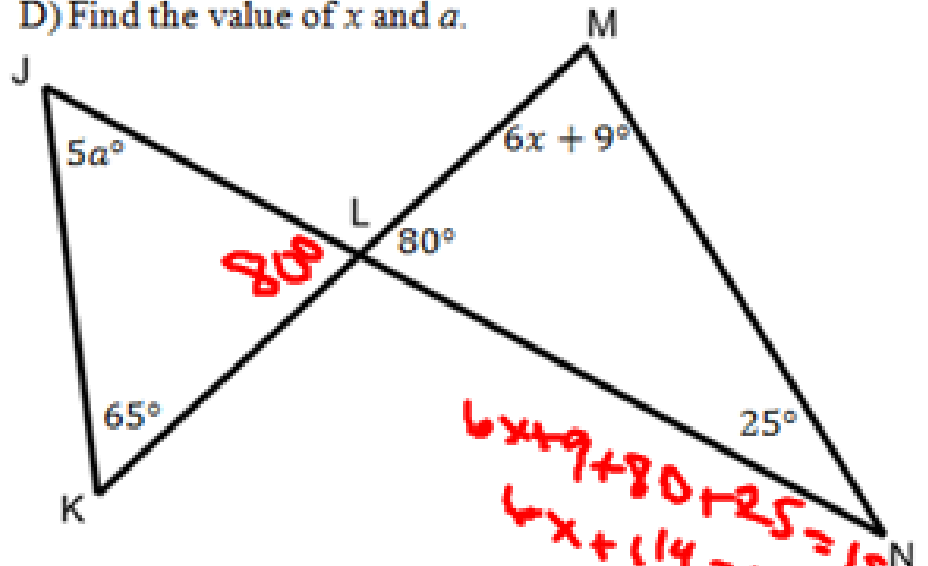
Equation  $\rightarrow 33 + 7x - 5 + 3x + 2 = 180$

$$10x + 30 = 180$$

$$\begin{array}{r} -30 \quad -30 \\ \hline 10x = 150 \\ \frac{10}{10} \quad \frac{150}{10} \end{array}$$

$x = \underline{15}$      $m\angle B = \underline{47^\circ}$      $x = 15$   
 $m\angle C = \underline{100^\circ}$

D) Find the value of  $x$  and  $a$ .



$x = \underline{11}$      $a = \underline{7}$      $m\angle M = \underline{75^\circ}$   
 $m\angle J = \underline{35^\circ}$      $m\angle KLN = \underline{80^\circ}$

$5a + 80 + 65 = 180$

$5a + 145 = 180$

$5a = 35$

$a = 7$